

Turbomachinery

Axial Compressors

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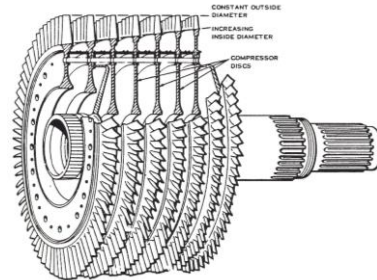
Cascade Flow Angles and Velocity Triangles

Compressor Analysis

- From Euler turbomachinery (conservation) equations need to understand change in tangential velocity to relate to forces on blades and power

$$T = \dot{m} \Delta(rc_\theta)$$

$$\dot{W} / \dot{m} = \Delta(uc_\theta)$$

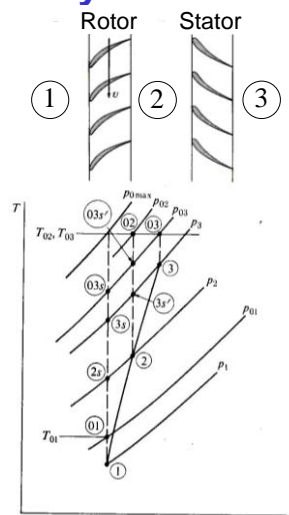


Mechanics and Thermodynamics of Propulsion, Hill and Peterson

- Analyze cascade flow to find values for c_θ (azimuthal or swirl velocity) through a compressor stage

Compressor Cascade Analysis

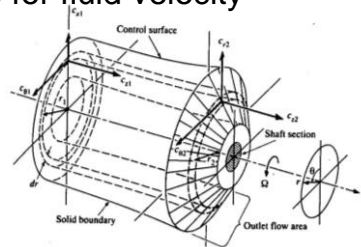
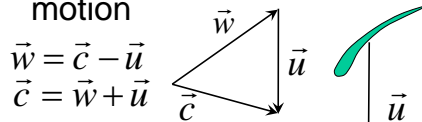
- Compressor stage consists of moving (rotor) and stationary (stator) blades
 - state change across each blade row
 - 1 → 2 rotor
 - 2 → 3 stator
- Use flow angles and velocity triangles to visualize transition between reference frames



Mechanics and Thermodynamics of Propulsion, Hill and Peterson

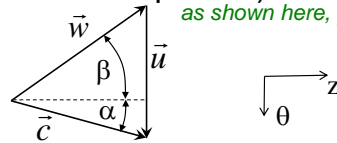
Compressor (Cascade) Flow Angles

- Recall, two reference frames for fluid velocity
 - engine's \vec{c}
 - blade's \vec{w}
- Difference due to rotor motion



"abs" swirl downward can still have swirl upward relative to rotor

- For cascade flow (no radial vel. component)
 - use u to define $+\theta$ dir.*
 - define angles for each ref. frame (α and β)



*sometimes (e.g., in UK) $\alpha > 0$ in U direction, $\beta > 0$ in opposite direction

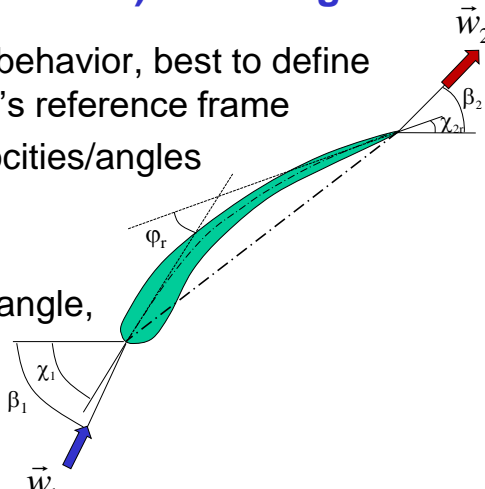
Compressor (Cascade) Flow Angles

- To examine airfoil behavior, best to define flow angle in blade's reference frame
- For **rotor**, use velocities/angles in rotating frame
 - w, β
 - net flow turning angle,

$$\beta_1 - \beta_2 \quad (II.9)$$

- will equal ϕ_r if flow matches blade angles

generally \neq , but could be close



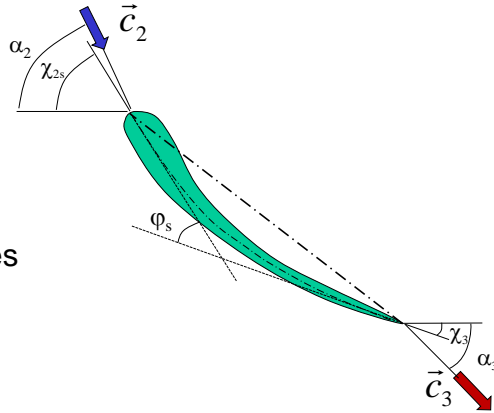
Compressor (Cascade) Flow Angles

- For **stator**, use engine reference frame

- c, α
- net flow turning angle,

$$\alpha_2 - \alpha_3 \quad (\text{II.10})$$

- will equal φ_s if flow matches blade angles
generally \neq , but could be close



Flow vs. Blade Angles

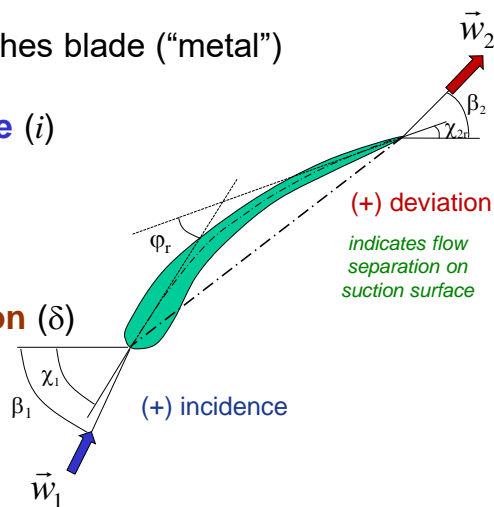
- How well flow matches blade (“metal”) angles is given by

- inflow: **incidence** (i)

$$\begin{aligned} i &\equiv -(\beta_1 - \chi_1) && \text{(rotor)} \\ i &\equiv \alpha_2 - \chi_{2s} && \text{(stator)} \end{aligned} \quad (\text{II.11})$$

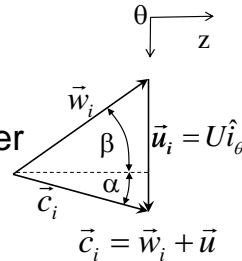
- outflow: **deviation** (δ)

$$\begin{aligned} \delta &\equiv -(\beta_2 - \chi_{2r}) && \text{(rotor)} \\ \delta &\equiv \alpha_3 - \chi_3 && \text{(stator)} \end{aligned} \quad (\text{II.12})$$



Velocity Triangles

- Rotor motion in θ direction, so ref. frame change has no effect on other directions $\Rightarrow w_{zi} = c_{zi}$ (II.13)



- Rotor vel. constant in cascade flow (like fixed r), and let $|u_i| = U$

$$\Rightarrow c_{\theta i} - w_{\theta i} = U \quad \text{as shown here, } w_{\theta} < 0 \quad \text{(II.14)}$$

- Also have general trigonometric relations

- e.g.,

$$\begin{aligned} c_{\theta i} &= c_i \sin \alpha_i = c_{zi} \tan \alpha_i \\ w_{\theta i} &= w_i \sin \beta_i = w_{zi} \tan \beta_i \\ w_{zi} &= w_i \cos \beta_i = c_{zi} = c_i \cos \alpha_i \end{aligned} \quad \text{(II.15)}$$

Velocity Triangle Analysis

- Apply (II.12-14) to both blade rows of compressor stage

- 1: rotor inlet

$$(13) \Rightarrow c_{\theta 1} = c_{z1} \tan \alpha_1$$

- 2: between rotor and stator

$$(13,15) \Rightarrow w_{\theta 2} = c_{z2} \tan \beta_2$$

$$(14) \Rightarrow c_{\theta 2} = U + w_{\theta 2}$$

$$c_{\theta 2} = U + c_{z2} \tan \beta_2 \quad \text{(II.16)}$$

$$\text{with (15)} \Rightarrow \tan \alpha_2 = \frac{U}{c_{z2}} + \tan \beta_2 \quad \text{(II.17)}$$

- 3: stator outlet

$$(15) \Rightarrow c_{\theta 3} = c_{z3} \tan \alpha_3$$

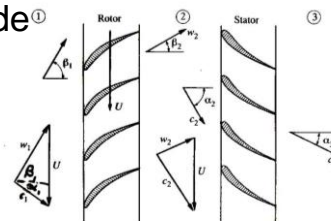


FIGURE 7.7 Mean radius section of a compressor stage. The absolute exit angle from *Mechanics and Thermodynamics of Propulsion*, Hill and Peterson

$$w_{zi} = c_{zi} \quad (13)$$

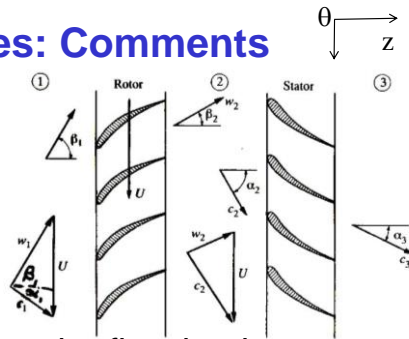
$$c_{\theta i} - w_{\theta i} = U \quad (14)$$

$$c_{\theta i} = c_i \sin \alpha_i = c_{zi} \tan \alpha_i$$

$$w_{\theta i} = w_i \sin \beta_i = w_{zi} \tan \beta_i \quad (15)$$

Velocity Triangles: Comments

- In axial compressor,
 - the rotor blades increase absolute swirl (push flow downward)
 - the stator blades reduce the swirl (return the flow back towards the axial direction)



Repeated (or Normal) Stage

≡ velocities at inlet and exit of stage are the same

$$(c_{z3}=c_{z1}, c_{\theta3}=c_{\theta1}, \alpha_3=\alpha_1)$$

Zero exit swirl

≡ no azimuthal velocity at exit of stage ($\alpha_3=0$)

Swirl Velocity Change Example

- **Given:**
 - Repeating axial flow compressor stage with pitchline radius of 0.50 m, rotational speed of 4050 rpm, inflow axial velocity of 155 m/s and inlet flow angle of 10.2° (in same direction as rotor wheel motion). The rotor blade exit angle is -22.5° and the deviation is 2° .
- **Find:**
 1. Change in swirl velocity across rotor ($\Delta c_{\theta 1,2}$)
 2. Change in swirl vel. ($\Delta c_{\theta 2,3}$) across stator
- **Assume:**
 - axial velocity constant through stage

Swirl Velocity Change Example

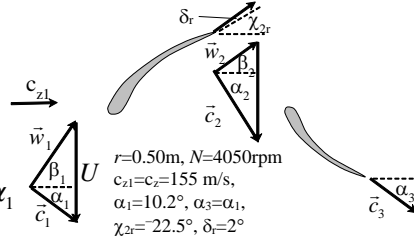
- $\Delta c_{\theta_{1,2}} = ?$

from (14) $c_{\theta_1} = c_{z_1} \tan \alpha_1$

from (15) $c_{\theta_2} = U + c_{z_2} \tan \beta_2$

$$c_{\theta_2} - c_{\theta_1} = U + c_{z_2} \tan \beta_2 - c_{z_1} \tan \alpha_1$$

$$\Delta c_{\theta_{1,2}} = U + c_z (\tan \beta_2 - \tan \alpha_1) \quad (\text{II.18})$$



Swirl Velocity Change Example

- $\Delta c_{\theta_{2,3}} = ?$

$$\Delta c_{\theta_{2,3}} = c_{\theta_3} - c_{\theta_2}$$

